

5.  $27^{x-1} = 3$

$$3^{3(x-1)} = 3^1$$

$$3(x-1) = 1$$

$$\frac{3x-3 = 1}{+3}$$

$$\frac{3x = 4}{\frac{3x}{3} = \frac{4}{3}}$$

$$x = \frac{4}{3}$$

6.  $64^{5x-4} = 2$

$$2^{6(5x-4)} = 2^1$$

$$6(5x-4) = 1$$

$$\frac{30x-24 = 1}{+24}$$

$$\frac{30x = 25}{\frac{30x}{30} = \frac{25}{30}}$$

$$x = \frac{5}{6}$$

7.  $2^{5x} = 8^{2x-1}$

$$2^{5x} = 2^{3(2x-1)}$$

$$5x = 6x - 3$$

$$\frac{-6x - 6x}{-x = -3}$$

$$x = 3$$

8.  $81^{2x-3} = 9^{x+3}$

$$9^2(2x-3) = 9^{x+3}$$

$$2(2x-3) = x+3$$

$$4x - 6 = x + 3$$

$$\frac{-x - x}{-x = 9}$$

$$\frac{3x - 6 = 9}{+6}$$

$$\frac{3x = 15}{\frac{3x}{3} = \frac{15}{3}}$$

$$x = 3$$

In the 1950s, scientists proposed a space station that could house a crew of approximately 80 people. The station could produce artificial gravity by rotating at a speed of  $w = \sqrt{gr}$  where  $g$  is 32 feet per second squared, and  $r$  is the radius of the station. If the station design required a rotating speed of approximately 64 feet per second to simulate gravity on Earth, what would the radius need to be?

$$w = \sqrt{gr}$$
$$(64)^2 = (\sqrt{32r})^2$$
$$\frac{4096}{32} = \frac{32r}{32}$$
$$128 = r$$