

Lesson 3.3 Part 2

Linear and Non-Linear Functions

A linear function is a function that has a graph that is a line. If the domain of the function is all real numbers, then the function is continuous. A linear equation can be used to describe a linear function.

Linear equations are often written in standard form.

Standard Form: $Ax + By = C$

- A is positive
- A, B, and C have a GCF of 1
- No fractions or decimals

$$y = mx + b$$

Also linear

$$\frac{2x}{2} + \frac{4y}{2} = \frac{6}{2}$$
$$x + 2y = 3$$

Examples

$$(2x)^2 \rightarrow (2x)(2x) \rightarrow 2 \cdot 2 \cdot x \cdot x$$

1. Determine whether $y = 4x^2 - (2x)^2 + 3x - 5$ is a linear or nonlinear function.

$$y = 4x^2 - 4x^2 + 3x - 5$$

$$y = 3x - 5 \quad \leftarrow \text{Slope-Intercept Form}$$

Linear

2. Determine whether $8 - 2y = x$ is a linear or nonlinear function.

$$\begin{array}{r} -8 \quad -8 \\ \hline -2y = x - 8 \\ -4 \quad -2 \quad -2 \end{array}$$

$$y = -\frac{1}{2}x + 4$$

Linear

3. Determine whether $y = 3x^3 - x^2 + 3x + 6$ is a linear or nonlinear function.

Not
because
exponents

4. Determine which of the equations below are linear or nonlinear

$$4x(2 - y) = 9$$

$$8x - 4xy = 9$$

Not

$$-3y = 5 - 2x$$

Linear

$$y = \frac{3}{4}x - \frac{1}{3}$$

Linear

$$y = \sqrt{2x - 4}$$

Not

$$y = 2x - \sqrt{4}$$

Linear

Functions in a Table

5. Salina kicks a soccer ball. The height of the ball after each half second is recorded in the table. Is the function that models the height of the ball a linear or nonlinear function?

Time (s)	Height (ft)
0	2
0.5	28
1	46
1.5	56
2	58
2.5	52
3	38
3.5	16

0.5

Look for slope

Not

6. Determine whether the values in each table are best modeled by a linear or nonlinear function.

Check for slope

x	y
-2	4
-1	1
0	0
1	1
2	4

Not

x	y
-2	8
1	-1
2	-4
5	-13
7	-19

$$\frac{\Delta y}{\Delta x} = \frac{-9}{3} = -\frac{3}{1}$$

$$\frac{-6}{2} = -\frac{3}{1}$$

Linear