

Systems Word Problems

$$y = Ax + By = c$$

1. A recreation center is offering special prices on its pool passes and gym memberships for the summer. On the first day of the offering, a family paid \$96 for 4 pool passes and 2 gym memberships. Later that day, an individual bought a pool pass for herself, a pool pass for a friend, and 1 gym membership. She paid \$72.

$$x = \text{pool} \quad y = \text{gym}$$

- a. Write a system of equations that represents the relationships between pool passes, gym memberships, and the costs. Be sure to state what each variable represents.

$$\begin{aligned} 96 &= 4x + 2y \\ 72 &= 2x + y \end{aligned} \rightarrow \begin{aligned} 96 &= 4x + 2y \\ 144 &= 4x + 2y \end{aligned}$$

- b. Find the price of a pool pass and the price of a gym membership by solving the system algebraically.

No Solution

2. A large pizza at Palanzio's Pizzeria costs \$6.80 plus \$0.90 for each topping. The cost of a large cheese pizza at Guido's Pizza is \$7.30 plus \$0.65 for each topping. How many toppings need to be added to a large cheese pizza from Palanzio's Pizzeria and Guido's Pizza in order for the pizzas to cost the same, not including tax?

$$\begin{aligned} x &: \text{Toppings} \\ y &: \text{Total Cost} \end{aligned}$$

$$y = 6.8 + 0.9x \quad (2, 8.6)$$

$$y = 7.3 + 0.65x$$

2 toppings

3. The length of a rectangle is equal to triple the width. If the perimeter is 86 centimeters, what are the dimensions of the rectangle?

L: Length

w: width

$$\begin{cases} 2L + 2w = 86 \\ L = 3w \end{cases}$$

$$P = L + L + w + w$$

$$2(3w) + 2w = 86$$

$$6w + 2w = 86$$

$$\frac{8w = 86}{8} \rightarrow w = 10.75$$

$$L = 3(10.75) \\ L = 32.25$$

Systems Word Problems

1. Monica and Michael both want to buy a scooter. Monica has already saved \$25 and plans to save \$5 per week. Michael has \$16 and plans to save \$8 per week. How many weeks will it take them to have saved the same amount and what is that amount?

x : Weeks
 y : Total \$

$$y = 5x + 25$$

$$y = 8x + 16$$

2. The sum of two numbers is 48 and their difference is 24. What are the two numbers?

$$\begin{array}{r} x + y = 48 \\ + x - y = 24 \\ \hline \end{array}$$

$$2x = 72$$

$$x = 36$$

$$y = 12$$

3. The length of Sally's garden is 4 meters greater than 3 times the width. The perimeter of the garden is 72 meters. What are the dimensions?

$$L = 3w + 4$$

$$2L + 2w = 72$$

4. Hank has a total of \$175 in \$5 and \$20 bills. The number of \$5 bills he has is 3 more than 4 times the number of \$20 bills. How many of each type of bill does Hank have?

x : \$5

y

$$5x + 20y = 175$$

y : \$20

$$x = 4y + 3$$

5. Leo is 38 years older than Adam. Five times Adam's age, when decreased by 5 is 1 more than Leo's age. How old is each?

L : Leo's Age

A : Adam's Age

$$L = A + 38$$

$$5A - 5 = L + 1$$

$$\begin{array}{r} 5A - 5 = A + 39 \\ A \quad A \end{array}$$